General Procedures for the Synthesis of Pyrido[2,3-d]pyrimidines 7-9 from the Reaction of Cyano Olefins 1-3 and 6-Aminouracil 4 or 6-(Hydroxyamino)uracil 5. A solution of 1.55 g (10 mmol) of 4a and 4.62 g (30 mmol) of cyano olefin (1a) in 50 mL of 1-propanol was refluxed for 4 h. The reaction mixture was concentrated to half of its volume, cooled, and filtered. Recrystallization from ethanol gave light brown crystals of 7a (2.82 g, 92%): mp 308-312 °C; ¹H NMR (CDCl₃) δ 2.90 (s, 3 H), 3.42 (s, 3 H), 6.78–7.25 (m, 5 H); IR 3435, 3300, 2195, 1710 cm⁻¹; MS 307 (M⁺).

Evaporation of the filtrate from 7a followed by column chromatography on silica gel column (benzene) gave benzylmalononitrile (1.48 g, 95%): mp 90-92 °C (lit.²² mp 91-92 °C); ¹H NMR (CDCl₃) δ 3.15 (d, 2 H), 3.70 (t, 1 H), 7.18 (m, 5 H); IR 2250 cm⁻¹; MS 153 (M⁺).

General Procedure for the Synthesis of Pyrazolo[3,4d]pyrimidine 10 from the Reaction of Cyano Olefins 1-3 and 6-Hydrazinouracil 6. A solution of 1.70 g (10 mmol) of 6a and 4.62 g (30 mmol) of cyano olefin 1a in 50 mL of 1-propanol was refluxed for 3 h. The reaction mixture was concentrated, cooled, and filtered. Recrystallization from ethanol gave 10a (2.30 g, 90%): mp 258-259 °C; ¹H NMR (TFA) δ 2.95 (s, 3 H), 3.40 (s, 3 H), 6.75-7.20 (m, 5 H); IR 3220, 1700 cm⁻¹; MS 256 (M⁺). Evaporation of the solvent from the filtrate of 7a in vacuo and column chromatography on a silica gel column (benzene-petroleum ether) gave malononitrile (0.60 g, 90%) [mp 32–34 °C; bp 220 °C] and ben-zylmalononitrile (1.51 g, 97%): mp 90–92 °C; ¹H NMR (CDCl₃) δ 3.15 (d, 2 H), 3.70 (t, 1 H), 7.18 (m, 5 H); IR 2250 cm⁻¹; MS 156 (M^+)

10b: vield 92%; mp 235-236 °C; ¹H NMR (TFA) δ 3.00 (s, 3 H), 3.45 (s, 3 H), 6.35–6.65 (m, 2 H), 7.25 (d, 1 H); IR 3225, 1705 cm^{-1} ; MS 246 (M⁺).

10c: yield 92%; mp 243-244 °C; ¹H NMR (TFA) δ 3.10 (s, 3

H), 3.50 (s, 3 H), 6.25–6.45 (m, 2 H), 7.15 (d, 1 H); IR 3220, 1705 cm⁻¹; MS 262 (M⁺).

10d: yield 82%; mp 256-257 °C; ¹H NMR (TFA) δ 2.95 (s, 3 H), 6.80-7.25 (m, 5 H); IR 3250, 3125, 1700 cm⁻¹; MS 242 (M⁺).

10e: yield 84%; mp 242-243 °C; ¹H NMR (TFA) δ 3.00 (s, 3 H), 6.30–6.45 (m, 2 H), 7.10 (d, 1 H); IR 3245, 3120, 1695 cm⁻¹; MS 232 (M⁺)

10f: yield 87%; mp 257-258 °C; ¹H NMR (TFA) δ 3.05 (s, 3 H), 6.35–6.50 (m, 2 H), 7.15 (d, 1 H); IR 3245, 3115, 1700 cm⁻¹; MS 248 (M⁺).

Synthesis of Pyrazolo[3,4-d]pyrimidine 10 from Reaction of 6 and 1 in Aprotic Solvent. A solution of 1.70 g (10 mmol) of 6a and 3.08 g (20 mmol) of 1a in 50 mL of dry DMF was heated at 125–130 °C for 2 h. The solvent was removed from the reaction mixture in vacuo, treated with water (75 mL), and filtered. Recrystallization of the crude compound from ethanol gave 10a (2.18 g, 85%): mp 258-259 °C. Column chromatography of the residue obtained from the evaporation of the filtrate gave malononitrile (0.58 g, 88%), mp 32-34 °C, and benzylmalononitrile (1.48 g, 95%), mp 90-92 °C.

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Registry No. 1a, 2700-22-3; 1b, 3237-22-7; 1c, 28162-32-5; 2a, 2025-40-3; 2b, 23973-22-0; 2c, 31330-51-5; 3a, 709-79-5; 3b, 3695-90-7; 3c, 54688-95-8; 4a, 6642-31-5; 4b, 21236-97-5; 5a, 42963-41-7; 5b, 123506-39-8; 6a, 123506-40-1; 6b, 123506-41-2; 7a, 95548-64-4; 7b, 123506-42-3; 7c, 123506-43-4; 7d, 95548-68-8; 7e, 123506-44-5; 7f, 123506-45-6; 8a, 123506-46-7; 8b, 123506-47-8; 8c, 123506-48-9; 8d, 123506-49-0; 8e, 123506-50-3; 8f, 123506-51-4; 9a, 123506-52-5; 9b, 123506-53-6; 9c, 123506-54-7; 9d, 123506-55-8; 9e, 123506-56-9; 9f, 123506-57-0; 10a, 35221-08-0; 10b, 123506-58-1; 10c, 123506-59-2; 10d, 42748-33-4; 10e, 123506-60-5; 10f, 123506-61-6; PhCH₂CH(CN)₂, 1867-37-4.

Synthesis of 6*H*-Pyrrolo[1,2-*c*][1,2,3]triazoles and 5H-Pyrrolo[1,2-d]tetrazoles: Alkylation and Acylation of the Monoanions

Jean-Pierre Dulcere,* Mohamed Tawil, and Maurice Santelli

Laboratoire Associé au CNRS, Centre de St-Jérôme, 13397 Marseille Cedex 13, France

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Thermal cyclization of 1-azido-2-penten-4-ynes and 4-azido-2-butenenitriles led to 6H-pyrrolo[1,2-c][1,2,3]triazoles and 5H-pyrrolo[1,2-d]tetrazoles, respectively, in good yields. Upon treatment with methyllithium these heterocyclic compounds gave the corresponding aromatic anions which can be alkylated with methyl iodide or acylated with ethyl chloroformate.

Unlike pentalene itself,¹ the corresponding pentalene dianion resulting from the addition of two electrons to the π -system is a stable material belonging to the class of aromatic compounds.² Ten general types of neutral heterocyclic systems have been recognized which are isoelectronic with the 10 π -electron system of the pentalenyl dianion.³ Six of these can be represented by a covalent formulation, whereas only mesomeric betaine structures

can be written for the four others. Several azapentalene anions have been prepared in solution as their lithium salts by deprotonation of the appropriate neutral compounds. The NMR spectra of these anions suggest that the negative charge is delocalized in a 10 π -electron system.³⁴ However little work has been devoted to the reactivity of these monoanions.4,5

In preliminary communications,⁶ we reported that 1azido-2-penten-4-ynes (2) can be thermally cyclized to a

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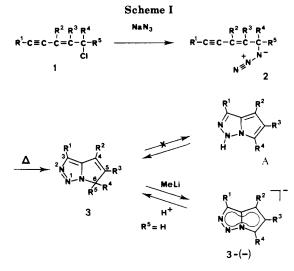
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a: $R^2 = CH_3$; $R^1 = R^3 = R^4 = R^5 = H$ **b**: $R^1 = R^2 = CH_3$; $R^3 =$ $\mathbf{R}^4 = \mathbf{R}^5 = \mathbf{H}$ c: $R^2 = R^3 = CH_3$; $R^1 = R^4 = R^5 = H$ d: $R^2 = R^3 = R^4 = CH_3$; $\mathbf{R}^1 = \mathbf{R}^5 = \mathbf{H}$ e: $R^2 = R^4 = R^5 = CH_3$; $R^1 = R^3 = H$ f: $R^2R^3 = -(CH_2)_4$ -; $R^4 = CH_3$; $R^1 = R^5 = H$

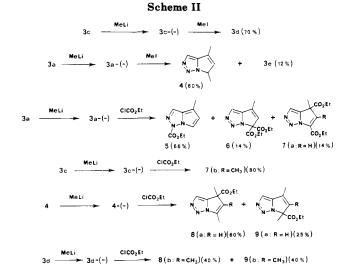
new class of azapentalene derivatives, the 6H-pyrrolo-[1,2-c] [1,2,3] triazoles (3). We describe here the extension of the scope of this reaction to the preparation of 5Hpyrrolo[1,2-d] tetrazoles (15) by the thermal cyclization of 4-azido-2-butenenitriles (14). The alkylation and the acylation of the 10 π -electron monoanions of 3 and 15 should offer a useful synthetic route to potentially bioactive heterocyclic compounds.⁷

Results

Azido enynes 2 are obtained in good yields by treatment of 1-chloro-2-penten-4-ynes 1^8 with an aqueous solution of sodium azide. Heating a benzene solution of azides 2 results in the formation of the pyrrolotriazoles 3. In this cycloaddition process the Z isomer of 2 is consumed, leaving behind unreacted E isomer⁹ (azidoenyne 2e cannot be isolated owing to its spontaneous cyclization to give 3e).¹⁰

The anions of 3a and 3c were generated by reaction with methyllithium in THF at -20 °C.¹³ The protonation of

butyllithium adds to the 5-position.



these anions regenerated starting 3a and 3c, respectively.

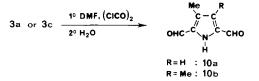
In particular, the formation of the tautomeric 1Hpyrrolo[1,2-c][1,2,3]triazoles A with a 10 π -electron conjugated system is not observed (Scheme I).¹⁴ Likewise alkylation of these anions with methyl iodide occurs exclusively at the 6-position to give 4 and 3d, respectively. A minor amount of the dimethylation produt 3e is also observed from 3a (Scheme II).

In contrast, acylation of the anions derived from 3 with ethyl chloroformate is less regioselective and takes place at the 1-, 4-, and 6-positions according to the substrate. The major product from 3a is the N-acylated heterocycle 5, which is particularly interesting, since a potentially aromatic structure is observed for the first time. This material undergoes spontaneous hydrolysis to regenerate 3a and must be protected from moisture.

Evidence for aromaticity of 5 is found in its NMR spectrum, which shows the protons at C(3), C(5), and C(6)at relatively low field (δ 7.66, 7.57, and 6.32 ppm, respectively).

The anion derived from 3c gives mainly the diacylated product 7b resulting from reaction at both C(4) and C(6). The second acylation is undoubtedly facilitated by the increased acidity of the monoacyalted intermediate. Compounds 4 and 3d are converted in a similar manner into mixtures of monoacylated products by substitution at C(6) and C(4), namely 8a, 9a and 8b, 9b, respectively.

An attempt to acylate triazole 3a and 3c with the Vilsmeier reagent¹⁵ leads to formylation of the pyrrole ring with concomitant loss of nitrogen. The formation of dialdehyde 10 in this process surely results from electrophilic attack on the 1H tautomers A of the starting materials.



Isomeric mixtures of chlorobutenenitriles 12 and 13 are obtained from cyanohydrins 11^{16,17} by exposure to the

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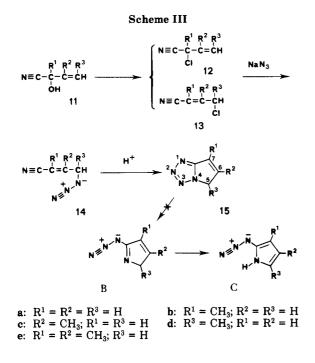
⁽¹⁰⁾ Although the intermolecular cycloaddition of an azide group to an acetylenic bond is a well-known process (see ref 11), few examples of

<sup>an acceptent bond is a well-known process (see 111), few examples of intramolecular additions have been reported previously (see ref 12).
(11) For a review, see: (a) Lwowski, W. 1,3-Dipolar Cycloaddition Chemistry; Padwa, A., Ed.; Wiley: New York, 1984; Vol. 1, pp 559–651.
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Vilsmeier reagent.^{15,18} Substitution with sodium azide occurs in good yield (80-85%) to give 4-azido-2-butenenitriles 14. Azides add with more difficulty to nitriles than to olefins or acetylenes.^{11a,19} In general, unactivated nitriles react with azides only when the two functions are incorporated into the same molecule,²⁰ and acid catalysis is necessary for the cycloaddition.²¹ Thus, heating 14b,c,e in the presence of chlorosulfonic acid proceeds smoothly to the pyrrolotetrazoles 15b,c.e. These compounds constitute a new class of fused-ring heterocycles.²² Azidonitriles 14a (E:Z = 7:3) and 14d (E isomer only) do not lead to the corresponding pyrrolotetrazoles, probably because of their unfavorable stereochemistry.

In the case of 15, an azidoazole–azolotetrazole isomer-ization is possible.^{4,23,24} Thus, the initial cycloadducts 5H-pyrrolo[1,2-d]tetrazoles could, in principle, equilibrate with the alternate open-chain valence tautomers 2-azido-

(18) Iminium salts are known to react with compounds with labile hydrogens to give substitution products. But, formation of formates will be avoided by slow hydrolysis; see: (a) Hepburn, D. R.; Hudson, H. R. J. Chem. Soc. Perkin Trans. 1 1976, 754. (b) Yoshihara, M.; Eda, T.; Sakaki, K.; Maeshima, T. Synthesis 1980, 746.

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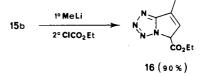
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isopyrroles B which could in turn undergo a favored tautomerism to 2-azidopyrroles C (Scheme III). In general the tendency for the formation of tetrazoles fused to a five-membered heterocycle from an azidoazole is low.²³ However, pyrrolotetrazoles 15 exhibit good thermal stability.25

Treatment of 15b by NaH in DMSO leads to the corresponding anion which has been examined by proton and carbon NMR. This data is consistent with an aromatic structure, particularly the deshielded H-C(5) proton at 6.6 ppm and the C(5) carbon at 90.5 ppm in addition to the other ring carbons at 146.8 and 115 ppm. Interestingly acylation of this anion occurs exclusively at the C(5)position.



In conclusion, the cyclization of azido enynes or azidobutenenitriles respectively offers an efficient synthesis of pyrrolotriazoles or pyrrolotetrazoles. The easy formation of corresponding anions allows the preparation of several substituted derivatives.

Experimental Section

General Methods. ¹H NMR spectra were determined on Varian EM 360 or Varian XL 200 spectrometers and were recorded for CDCl₃ (or CCl₄) solutions containing Me₄Si as the internal Standard. ¹³C NMR spectra of CDCl₃ solutions were recorded on a Varian XL 200 (50.309 MHz) spectrometer with Me₄Si as the internal standard. Assignments were confirmed by J-modulated spin echo. Mass spectra were obtained on a Varian MAT 311 mass spectrometer. Melting points are uncorrected. All reactions were carried out in an argon atmosphere.

Materials. 1-Chloro-2-penten-4-ynes (1) were prepared according to the reported method.^{8b} Cyanhydrins 11a,b,c,e were prepared by addition of cyanide anion to conjugated ethylenic aldehydes or ketones;¹⁶ cyanhydrin 11d was obtained by hydrolysis of the trimethylsilyl derivative.¹⁷ Yields were as follows: 2hydroxy-3-butenenitrile (11a), 61%; 2-hydroxy-2-methyl-3-butenenitrile (11b), 50%; 2-hydroxy-3-methyl-3-butenenitrile (11c), 88%; 2-hydroxy-3-pentenenitrile (11d), 92%; 2-hydroxy-2,3-dimethyl-3-butenenitrile (11e), 20%.

General Procedure for the Preparation of 6H-Pyrrolo-[1,2-c][1,2,3]triazoles (3). Sodium azide (8.45 g, 130 mmol) was dissolved in water (20 mL) and 1-chloro-2-penten-3-ynes (1) were added (50 mmol). The mixture was stirred for 24 h. The azido enynes 2 were extracted by pentane. The organic layer was dried (MgSO₄) and concentrated in vacuo. The crude azido envnes were dissolved in benzene (500 mL). After refluxing (5 h), the solution was concentrated under reduced pressure to yield the crude triazole. Pure triazoles 3 were isolated by recrystallization from chloroform-pentane (1/4) or by chromatography on silica gel.

4-Methyl-6H-pyrrolo[1,2-c][1,2,3]triazole (3a). General procedure with 1-chloro-3-methyl-2-penten-4-yne (1a) (5.72 g): The benzene solution of the crude azido enyne (2a) was refluxed 4 h to give 3a (4.35 g, 72%): mp 73 °C, picrate mp 128 °C; IR $(CDCl_3)$ 1615, 815 cm⁻¹; ¹H NMR δ 7.40 (1, s), 6.25 (1, m, $W_{1/2}$ = 4 Hz), 4.73 (2, m, $W_{1/2}$ = 6 Hz), 2.13 (3, d, J = 2 Hz); ¹³C NMR δ 146.7 (s), 129.7 (s), 128.4 (d), 122.4 (d), 51.1 (t), 13.3 (q); mass spectrum, m/e 122 (5), 121 (57), 93 (74), 67 (24), 66 (100), 65 (61), 40 (45), 39 (48); HRMS calcd for C₆H₇N₃ 121.0640, found 121.0636.

3,4-Dimethyl-6H-pyrrolo[1,2-c][1,2,3]triazole (3b). General procedure with 1-chloro-3-methyl-2-hexen-4-yne (1b) (6.42 g): The benzene solution of the crude azido enyne (2b) was refluxed 5

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h to give **3b** (oil), purified by chromatography on silica gel (ether-pentane) (5.94 g, 88%): IR 1615, 815 cm⁻¹; ¹H NMR (CCl₄) δ 6.15 (1, m, $W_{1/2}$ = 5 Hz), 4.73 (2, m, $W_{1/2}$ = 8 Hz), 2.36 (3, s), 2.16 (3, d, J = 2 Hz). Anal. Calcd for C₇H₉N₃: C, 62.22; H, 6.67; N, 31.11. Found: C, 62.40; H, 6.72; N, 30.89.

4,5-Dimethyl-6*H***-pyrrolo**[**1,2***c***3**]**(1,2**,3**)triazole (3c).** General procedure with 1-chloro-2,3-dimethyl-2-penten-4-yne (1c) (6.42 g): The benzene solution of crude **2c** was refluxed 1.5 h to give **3c** (5.26 g, 78%): mp 101 °C; picrate mp 132 °C; IR (CDCl₃) 1615, 815 cm⁻¹; ¹H NMR δ 7.28 (1, s), 4.63 (2, br s), 2.05 (6, br s); ¹³C NMR δ 147.8 (s), 138.4 (s), 122.2 (s), 121.3 (d ¹J_{CH} = 195.3 Hz), 12.2 (q), 10.4 (q); mass spectrum, *m/e* 136 (8), 135 (73), 107 (55), 106 (100), 79 (83), 77 (38), 65 (40), 39 (43); HRMS calcd for C₇H₉N₃ 135.0796, found 135.0802.

4,5,6-Trimethyl-6*H*-pyrrolo[1,2-*c*][1,2,3]triazole (3d). General procedure with 2-chloro-3,4-dimethyl-3-hexene-5-yne (1d) (7.12 g): The benzene solution of crude 2d was refluxed 8 h to give 3d as an oil, purified by chromatography on silica gel (eth-er-pentane) (5.21 g, 70%): picrate mp 138 °C; IR (CDCl₃) 1615, 810 cm⁻¹; ¹H NMR (CDCl₃) δ 7.29 (1, s), 4.60 (1, q, J = 7 Hz), 2.0 (6, m), 1.58 (3, d, J = 7 Hz). Anal. Calcd for C₈H₁₁N₃: C, 64.43; H, 7.38; N, 28.19. Found: C, 64.54; H, 7.25; N, 28.24.

4,6,6-Trimethyl-6H-pyrrolo[1,2-*c*][1,2,3]triazole (3e). General procedure with 2-chloro-2,4-dimethyl-3-hexen-5-yne (1e) (7.12 g): Crude azido enyne **2e** could not be isolated; spontaneous cyclization occured to give **3e** (6.70 g, 90%): bp 70 °C (1 Torr); picrate mp 142 °C; IR 1615, 810 cm⁻¹; ¹H NMR (CDCl₃) δ 7.4 (1, s), 6.4 (1, q, J = 1.8 Hz), 2.11 (3, d, J = 1.8 Hz), 1.61 (6, s). Anal. Calcd for C₈H₁₁N₃: C, 64.43; H, 7.38; N, 28.19. Found: C, 64.58; H, 7.30; N, 28.11.

6-Methyl-4,5-tetramethylene-6*H*-pyrrolo[1,2-*c*][1,2,3]triazole (3f). General procedure with 1f (8.42 g): The benzene solution of crude 2f was refluxed 5 h to give 3f as an oil, purified by chromatography on silica gel (ether-pentane) (8.05 g, 92%): picrate mp 149 °C; IR 1615, 810 cm⁻¹; ¹H NMR (CDCl₃) δ (7.38 1, s), 4.76 (1, q, J = 7 Hz), 2.33 (4, m), 1.76 (4, m), 1.6 (3, d, J =7 Hz). Anal. Calcd for C₁₀H₁₃N₃: C, 68.57; H, 7.43; N, 24.00. Found: C, 68.49; H, 7.40;, N, 24.12.

General Procedure for the Alkylation or the Acylation of Triazoles or Tetrazoles. To a stirred solution of the heterocycle (10 mmol) in anhydrous THF (25 mL), cooled to -60 °C was added methyllithium (12 mmol in ether). The solution was allowed to warm at -20 °C and stirred for 1 h. The solution was cooled to -60 °C, and methyl iodide (2.13 g, 15 mmol) or ethyl chloroformate (1.63 g, 15 mmol) was added. After 4 h of stirring, the mixture was poured into ice containing ether. After separation of layers, the aqueous phase was extracted with ether, and the combined organic layers were washed with brine and dried (MgSO₄). The solution was concentrated under reduced pressure, and the crude products were purified by chromatography on silica gel (ether-pentane).

Methylation of 3a. Alkylation of 3a (1.21 g) was performed with methyl iodide according to the general procedure. Two products were separated by chromatography on silica gel, 3e (12%) and 4,6-dimethyl-6H-pyrrolo[1,2-c][1,2,3]triazole (4) (60%): IR (CDCl₃) 1615, 810 cm⁻¹; ¹H NMR δ 7.40 (1, s), 6.22 (1, br s), 4.92 (1, q, J = 7 Hz), 2.15 (3, d, J = 1 Hz), 1.61 (3, d, J = 7 Hz). Anal. Calcd for C₇h₉N₃: C, 62.22; H, 6.67; N, 31.11. Found: C, 62.01; H, 6.77; N, 31.22.

Methylation of 3c. Alkylation of 3c (1.35 g) by methyl iodide led to 3d (65% yield).

Acylation of 3a. Acylation of 3a (1.21 g) by ethyl chloroformate (1.41 g, 13 mmol) led to a mixture of 1-(ethoxy-carbonyl)-4-methyl-1*H*-pyrrolo[1,2-*c*][1,2,3]triazole (5) (66%), 6,6-bis(ethoxycarbonyl)-4-methyl-6*H*-pyrrolo[1,2-*c*][1,2,3]triazole (6) (14%), and 4,6-bis(ethoxycarbonyl)-4-methyl-4*H*-pyrrolo[1,2-*c*][1,2,3]triazole (7a) (14%). Compound 5 showed: IR (CDCl₃) 1730, 880, 860 cm⁻¹; ¹H NMR δ 7.66 (1, s), 7.57 (1, d, J = 2.4 Hz), 6.32 (1, d, J = 2.4 Hz), 4.52 (2, q, J = 7.2 Hz), 2.27 (3, s), 1.47 (3, t, J = 7.2 Hz). Anal. Calcd for C₉H₁₁N₃O₂: C, 55.96; H, 5.70; N, 21.76. Found: C, 55.78; H, 5.60; N, 21.86. Compound 6 showed: mp 94 °C (chloroform-pentane); IR (CCl₄) 1730, 860 cm⁻¹; ¹H NMR (CCl₄) δ 7.32 (1, s), 6.24 (1, br s), 4.24 (2, q, J = 7.2 Hz), 2.21 (3, br s), 1.33 (3, t, J = 7.2 Hz); ¹³C NMR δ 162.9 (s) (2 C), 145.7 (s), 132.2 (s), 129.6 (d), 123.3 (d), 116.0 (s), 63.8 (t) (2 C), 13.9 (q) (2 C), 13.2 (q). Anal. Calcd

for C₁₂H₁₅N₃O₄: C, 54.34; H, 5.66; N, 15.85. Found: 54.46; H, 5.59; N, 15.77. Compound **7a** showed: IR (CCl₄) 1770, 1685, 855 cm⁻¹; ¹H NMR (CCl₄) δ 8.07 (1, s), 7.09 (1, s), 4.58 (2, q, *J* = 7.2 Hz), 4.33 (2, q, *J* = 7.2 Hz), 2.25 (3, s), 1.50 (3, t, *J* = 7.2 Hz), 1.38 (3, t, *J* = 7.2 Hz); ¹³C NMR δ 159.6 (s), 147.9 (s), 134.6 (s), 125.7 (d), 110.8 (d), 105.4 (s), 101.5 (s), 66.5 (t), 59.8 (t), 14.7 (q), 14.1 (q), 11.5 (q); mass spectrum, *m/e* 265 (49), 193 (22), 165 (37), 119 (100), 92 (63); HRMS calcd for C₁₂H₁₅N₃O₄ 265.1062, found 265.1040.

Acylation of 3c. Acylation of 3c (1.35 g) by ethyl chloroformate (2.39 g, 22 mmol) led to 4,6-bis(ethoxycarbonyl)-4,5dimethyl-4H-pyrrolo[1,2-c][1,2,3]triazole (7b) (80% yield): IR (CDCl₃) 1765, 1660 cm⁻¹; ¹H NMR δ 8.0 (1, s), 4.61 (2, q, J = 7.2 Hz), 4.39 (2, q, J = 7.2 Hz), 2.43 (3, s), 2.17 (3, s), 1.52 (3, t, J = 7.2 Hz), 1.42 (3, t, J = 7.2 Hz). Anal. Calcd for C₁₃H₁₇N₃O₄: C, 55.91; H, 6.09; N, 15.05. Found: C, 56.06; H, 6.18; N, 14.94.

Acylation of 4. Acylation of 4 (1.35 g) by ethyl chloroformate (1.42 g, 15 mmol) led to 4-(ethoxycarbonyl)-4,6-dimethyl-4H-pyrrolo[1,2-c][1,2,3]triazole (8a) (60%) and 6-(ethoxycarbonyl)-4,6-dimethyl-6H-pyrrolo[1,2-c][1,2,3]triazole (9a) (25%). Compound 8a showed: IR (CDCl₃) 1750, 820 cm⁻¹; ¹H NMR δ 7.65 (1, s), 6.00 (1, s), 4.41 (2, q, J = 7.2 Hz), 2.48 (3, s), 2.20 (3, s), 1.43 (3, t, J = 7.2 Hz); ¹³C NMR δ 151.6 (s), 134.4 (d), 128.5 (s), 126.3 (s), 116.0 (d), 106.6 (s), 64.5 (t), 14.3 (q), 14.0 (q), 11.1 (q). Anal. Calcd for C₁₀H₁₃N₃O₂: C, 57.97; H, 6.28; N, 20.29. Found: C, 57.88; H, 6.36; N, 20.34. Compound 9a showed: IR (CCl₄) 1740, 860 cm⁻¹; ¹H NMR (CCl₄) δ 7.31 (1, s), 6.22 (1, q, J = 1.8 Hz), 4.14 (2, q, J = 7.2 Hz), 2.15 (3, d, J = 1.8 Hz), 1.82 (3, s), 1.21 (3, t, J = 7.2 Hz). Anal. Calcd for C₁₀H₁₃N₃O₂: C, 57.97; H, 6.28; N, 20.29. Found: C, 57.84; H, 6.30; N, 20.38.

Acylation of 3d. Acylation of 3d (1.49 g) led to 4-(ethoxy-carbonyl)-4,5,6-trimethyl-4*H*-pyrrolo[1,2-*c*][1,2,3]triazole (8b) (40%) and 6-(ethoxycarbonyl)-4,5,6-trimethyl-6*H*-pyrrolo[1,2-*c*][1,2,3]triazole (9b) (40%). Compound 8b showed: IR (film) 1760, 1250 cm⁻¹; ¹H NMR (CCl₄) δ 7.47 (1, s), 4.34 (2, q, J = 7.2 Hz), 2.37 (3, s), 2.10 (3, s), 2.00 (3, s), 1.42 (3, t, J = 7.2 Hz); ¹³C NMR δ 152.0 (s), 134.3 (d), 127.5 (s), 124.5 (s), 122.2 (s), 105.6 (s), 64.5 (t), 14.4 (q), 12.1 (q), 9.7 (q), 9.6 (q). Anal. Calcd for C₁₁H₁₅N₃O₂: C, 59.72; H, 6.79; N, 19.00. Found: C, 59.63; H, 6.84; N, 18,89. Compound 9b showed: IR (film) 1760, 1260 cm⁻¹; ¹H NMR (CCl₄) δ 7.23 (1, br s), 4.10 (3, q, J = 7.2 Hz), 2.07 (3, d, J = 1.4 Hz), 1.95 (3, s), 1.79 (s), 1.17 (3, t, J = 7.2 Hz). Anal. Calcd for C₁₁H₁₅N₃O₂: C, 59.72; H, 6.79; N, 19.00. Found: C, 59.65; H, 6.76; N, 19.08.

Formylation of 3a and 3c. Vilsmeier salt $(28.5 \text{ mmol})^{15}$ in anhydrous CH₂Cl₂ (20 mL) was cooled and stirred at 0 °C. Triazole 3a or 3c (5 mmol) in anhydrous CH₂Cl₂ (30 mL) was added and stirred for 14 h. The reaction mixture was poured into ice and extracted with ether. The combined organic fractions were washed with brine and dried (MgSO₄). After concentration in vacuo, the crude product was recrystallized from chloroformpentane to give 10a (35% yield) [mp 83 °C; IR (CCl₄) 3300, 1670 cm⁻¹; ¹H NMR (CDCl₃) δ 9.56 (1, s), 9.39 (1, s), 6.53 (1, s), 2.3 (3, s); ¹³C NMR δ 181.3 (d), 180.4 (d), 134.7 (s), 132.5 (s), 130.9 (s), 120.5 (d), 10.6 (q). Anal. Calcd for C₇H₇NO₂: C, 61.31; H, 5.11; N, 10.21. Found: C, 61.36; H, 5.05; N, 10.27] or 10b (30% yield): mp 137-138 °C; IR (CCl₄) 1750, 1250 cm⁻¹; ¹H NMR (CDCl₃) δ 9.75 (2, s), 2.31 (6, s); ¹³C NMR δ 180.3 (d), 131.9 (s), 129.7 (s), 8.3 (q). Anal. Calcd for C₈H₉NO₂: C, 63.57; H, 5.96; N, 9.27. Found: C, 63.60; H, 5.85; N, 9.21.

General Procedure for the Preparation of Chlorobutenenitriles (12 or 13). Vilsmeier salt (40 mmol)^{15,18} in anhydrous acetonitrile (30 mL) was cooled to -20 °C and stirred. Cyanhydrin 11 (20 mmol) in anhydrous acetonitrile (20 mL) was slowly added. The reaction mixture was warmed to room temperature and stirred for 3 h. The reaction mixture was poured into ice and extracted with pentane. The layers were separated, and the aqueous fraction was extracted with pentane. The combined organic fractions were washed with brine and dried (MgSO₄). Concentration in vacuo and purification by chromatography on silica gel afforded 12 or 13. 2-Chloro-3-butenenitrile (12a) (53% yield): IR (film) cm⁻¹; ¹H NMR (CCl₄) δ 5.7-4.83 (3, m). 4-Chloro-2-methyl-2-butenenitrile (13b) (57% yield): IR (film) 2220 cm⁻¹; ¹H NMR (CCl₄) δ 5.97 (1, t, J = 7.2 Hz), 4.03 (2, d, J = 7.2 Hz), 1.96 (3, br s). 2-Chloro-3-methyl-3-butenenitrile (12c) (50% yield): IR (film) 2245, 925 cm⁻¹; ¹H NMR (CCl₄) δ 5.33 (1, br s), 5.13 (1, br s), 4.92 (1, br s), 1.97 (3, br s); ¹³C NMR δ 137.0 (s), 118.8 (t), 115.4 (s), 46.9 (d), 18.1 (q). 4- **Chloro-3-methyl-2-butenenitrile (13c)** (25% yield): IR (neat) 2225 cm⁻¹; ¹H NMR (CCl₄) δ 5.30 (1, s), 3.90 (2, s), 2.04 (3, s). *trans*-4-Chloro-2-pentenenitrile (13d) (50% yield): IR (film) 2215 cm⁻¹; ¹H NMR (CCl₄) δ 6.37 (1, dd, J = 16, 6.2 Hz), 5.57 (1, d, J = 16 Hz), 4.53 (1, quint, J = 6.2 Hz), 1.60 (3, d, J = 6.2 Hz); ¹³C NMR δ 153.4 (d), 116.3 (s), 100.9 (d), 54.4 (d), 23.8 (q). 4- **Chloro-2,3-dimethyl-2-butenenitrile (13e)** (45% yield): IR (film) 2215 cm⁻¹; ¹H NMR (CCl₄) δZ isomer 4.16 (2, s), 1.93 (6, br s); E isomer 3.96 (2, s), 1.93 (6, br s).

General Procedure for 4-Azido-2-butenenitriles (14). The same procedure as for azidopentenynes 2 was used and the crude product was purified by chromatography on silica gel (etherpentane). 4-Azido-2-butenenitrile (14a) (82% yield) (mixture of E/Z isomers, 7:3): IR (film) 2220, 2100 cm⁻¹; E isomer ¹H NMR δ 6.63 (1, dt, J = 16.2, 4.65 Hz), 5.60 (1, dt, J = 16.2, 2 Hz), 4.00 $(2, dd, J = 4.6, Hz, 2 Hz); {}^{13}C NMR \delta 147.3 (d), 116.5 (s), 102.0$ (d), 51.3 (t); Z isomer ¹H NMR δ 6.46 (1, dt, J = 11, 5.5 Hz), 5.54 $(1, dt, J = 11, 1.4 Hz), 4.10 (2, d, J = 6.4 Hz, d, J = 2.8 Hz); {}^{13}C$ NMR δ 146.6 (d), 114.1 (s), 103.1 (d), 50.2 (t). (Z)-4-Azido-2methyl-2-butenenitrile (14b) (85% yield): IR (film) 2210, 2090 cm⁻¹; ¹H NMR (CCl₄) δ 6.09 (1, t, J = 7.2 Hz), 3.99 (2, d, J = 7.2 Hz), 2.04 (3, br s). 4-Azido-3-methyl-2-butenenitrile (14c) (80% yield) (72:28 mixture of E/Z isomers): IR 2225, 2120 cm⁻¹; ¹H NMR (CCl₄) δ E isomer 5.38 (1, br s), 3.93 (2, br s), 2.05 (3, br s); Z isomer 5.30 (1, br s), 4.06 (2, br s), 2.05 (3, br s). trans-4-Azido-2-pentenenitrile (14d) (80% yield): IR (film) 2225, 2150 cm⁻¹; ¹H NMR (CCl₄) δ 6.47 (1, d, J = 16, 5.5 Hz), 5.47 (1, d, J= 16 Hz), 4.10 (1, quint, J = 6 Hz), 1.33 (3, d, J = 6 Hz). 4-Azido-2,3-dimethyl-2-butenenitrile (14e) (82% yield) (29:71 mixture of E/Z isomers): IR (film) 2210, 2100 cm⁻¹; ¹H NMR $(CCl_4) \delta E$ isomer 3.85 (2, s), 1.89 (6, br s); Z isomer 3.98 (2, s), 1.89 (6 br s).

General Procedure for Tetrazoles (15). A solution of azidobutenenitrile (14) (5 mmol) in chloroform (30 mL) was treated at room temperature with chlorosulfonic acid (1.16 g, 10 mmol). After 0.5 h of stirring, the mixture was washed with a saturated solution of NaHCO₃ and dried (MgSO₄). After concentration in vacuo, the crude product was recrystallized from chloroform-pentane (1:4).

7-Methyl-5*H***-pyrrolo[1,2-***d***]tetrazole (15b). General procedure with 14b gives 15b (0.61 g) (57% yield): mp 113 °C; IR (CDCl₃) 1520, 1460, 1245 cm⁻¹; ¹H NMR \delta 6.65 (1, t, J = 7.2 Hz), 4.78 (2, d, J = 7.2 Hz), 2.30 (3, s); ¹³C NMR \delta 164.0 (s), 135.0 (d), 127.9 (s), 50.3 (t), 12.4 (q); mass spectrum, m/e 123 (12), 122 (100), 94 (24), 93 (15), 79 (35), 66 (60), 65 (64), 39 (83); HRMS calcd for C₅H₆N₄ 122.0592, found 122.0584.**

6-Methyl-5H-pyrrolo[1,2-*d*]**tetrazole (15c).** General procedure with 14c gives 15c (0.61 g) (25% yield): mp 104 °C; IR (CDCl₃) 1530, 1460 cm⁻¹; ¹H NMR δ 6.50 (1, br s, $W_{1/2}$ = 4 Hz), 4.73 (2, br s), 2.28 (3, s); ¹³C NMR δ 164.2 (s), 154.7 (s), 112.5 (d), 53.5 (t), 16.0 (q). Anal. Calcd for C₅H₆N₄: C, 49.18; H, 4.92; N, 45.90. Found: C, 49.06; H, 4.73; N, 46.04.

6,7-Dimethyl-5*H*-**pyrrolo**[**1,2-***d*]**tetrazole** (15e). General procedure with 14e gives 15e (0.68 g) (73% yield): mp 95 °C; IR (CDCl₃) 1530, 1460 cm⁻¹; ¹H NMR δ 4.74 (2, s), 2.19 (6, br s); ¹³C NMR δ 164.6 (s), 132.9 (s), 120.8 (s), 53.1 (t), 13.0 (q), 9.7 (q); mass spectrum, m/e 137 (12), 136 (95), 108 (26), 80 (31), 79 (100), 77 (32), 67 (30), 53 (30), 40 (66); HRMS calcd for C₆H₈N₄ 136.0749, found 136.0753.

Formation of the Anion of 15b. Sodium hydride (30 mg) was added to a solution of 8b (150 mg) in DMSO- d_6 (3 mL) in a 10-mm NMR tube. The NMR spectra were recorded after 10 min: ¹H NMR δ 6.62 (1, m), 6.10 (1, m), 2.1 (3, br s); ¹³C NMR δ 146.5 (s), 115.0 (d), 90.5 (d), 79.1 (s), 12.1 (q).

Acylation of 15b. Acylation of 15b (1.22 g) by ethyl chloroformate (1.42 g, 15 mmol) led to 5-(ethoxycarbonyl)-7-methyl-5H-pyrrolo[1,2-d]tetrazole (16) (76%): mp 58–59 °C (chloroform-pentane); IR (CCl₄) 1750, 1250 cm⁻¹; ¹H NMR δ 6.69 (1, d, J = 3.5 Hz), 6.20 (1, d, J = 3.5 Hz), 4.38 (2, J = 7.2 Hz), 2.19 (3, s), 1.38 (3, t, J = 7.2 Hz); ¹³C NMR δ 165.7 (s), 147.3 (s), 127.7 (s), 120.9 (d), 102.2 (d), 65.1 (t), 14.0 (q), 10.7 (q); mass spectrum, m/e 195 (10), 194 (63), 168 (10), 150 (10), 143 (57), 122 (100), 93 (75), 67 (72), 41 (56); HRMS calcd for C₈H₁₀N₄O₂ 194.0803, found 194.0796.

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Registry No. 1a, 123810-18-4; 1b, 123810-19-5; 1c, 123810-20-8; 1d, 123810-21-9; 1e, 123810-22-0; 1f, 38264-11-8; 2a, 64803-97-0; 2b, 64803-99-2; 2c, 64803-96-9; 2d, 64803-98-1; 2e, 123810-23-1; 2f, 64804-00-8; 3a, 64804-02-0; 3b, 64804-04-2; 3c, 64804-01-9; 3d, 64804-03-1; 3e, 30435-17-7; 3f, 64804-05-3; 4, 123810-24-2; 5, 123810-25-3; 6, 123810-26-4; 7a, 123810-27-5; 7b, 123810-28-6; 8a, 123810-29-7; 8b, 123810-26-4; 7a, 123810-27-5; 7b, 123810-28-6; 8a, 123810-29-7; 8b, 123810-31-1; 9a, 123810-30-0; 9b, 123810-32-2; 10a, 90935-74-3; 10b, 51952-99-9; 11a, 5809-59-6; 11b, 75819-97-5; 11c, 22410-56-6; 11d, 6812-26-6; 11e, 4346-65-0; 12a, 24253-31-4; 12c, 123810-33-3; 13b, 92089-38-8; 13c, 4450-34-4; 13d, 123810-34-4; (Z)-13e, 123810-35-5; (E)-13e, 26157-52-8; (E)-14a, 123810-34-4; (Z)-14a, 123810-37-7; (Z)-14b, 123810-38-8; (E)-14c, 123810-39-9; (Z)-14c, 123810-40-2; (E)-14d, 120990-04-7; (E)-14e, 123810-41-3; (Z)-14e, 123810-42-4; 15b, 123810-43-5; 15b (anion), 123810-46-8; 15c, 123810-44-6; 15e, 123810-45-7; 16, 123834-20-8.

β -Lactams via α,β -Unsaturated Acid Chlorides: Intermediates for Carbapenem Antibiotics¹

M. S. Manhas,* Malay Ghosh, and Ajay K. Bose

Department of Chemistry and Chemical Engineering, Stevens Institute of Technology, Hoboken, New Jersey 07030

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Stereocontrolled synthesis of α -vinyl β -lactams and their transformation to convenient intermediates for PS-5, PS-6, asparenomycin, and thienamycin are described.

Introduction

The acid chloride-imine reaction has been used extensively to synthesize various substituted β -lactams.²

Azidoacetyl chloride-imine cycloaddition, also known as the Bose reaction,³ has been used as a pivotal synthetic

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